



## FADEX

October 16th, 2023  
Nancy, France

# Preventing Timing Leaks using Parametric Timed Model Checking

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Based on joint works with Étienne André, Shapagat Bolat, Engel Lefauchaux, Didier Lime, and Sun Jun

These works are partially supported by the ANR-NRF research program ProMiS (ANR-19-CE25-0015) and the ANR research program BisoUS (ANR-22-CE48-0012).



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  - ▶ Number of pizzas (and order time) ordered by the white house prior to major war announcements <sup>1</sup>

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pwd c h i c k e n

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Execution time:  $\epsilon + \epsilon + \epsilon$

- ▶ **Problem:** The execution time is proportional to the number of consecutive correct characters from the beginning of attempt

# Timing attacks

- ▶ Principle: deduce **private information** from timing data (**execution time**)

Issues:

- ▶ May depend on the **implementation** (or, even worse, be **introduced by the compiler**)
- ▶ A relatively trivial solution: make the program last always its maximum execution time  
Drawback: **loss of efficiency**

~> Non-trivial problem

# Detection

Need to detect timing-leak vulnerabilities

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We want formal guarantees → formal methods

- ▶ Various methods:
  - ▶ Abstract interpretation
  - ▶ Static analysis
  - ▶ Model checking
  - ▶ Theorem proving



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  - ▶ Static analysis
  - ▶ **Model checking**
  - ▶ Theorem proving



# Methodology

A program

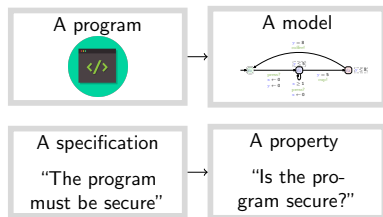


A specification

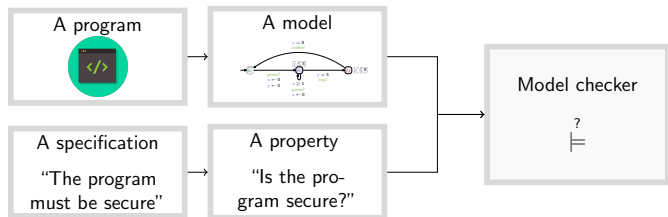
“The program  
must be secure”



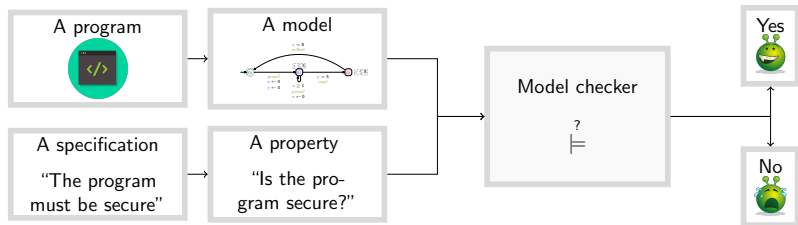
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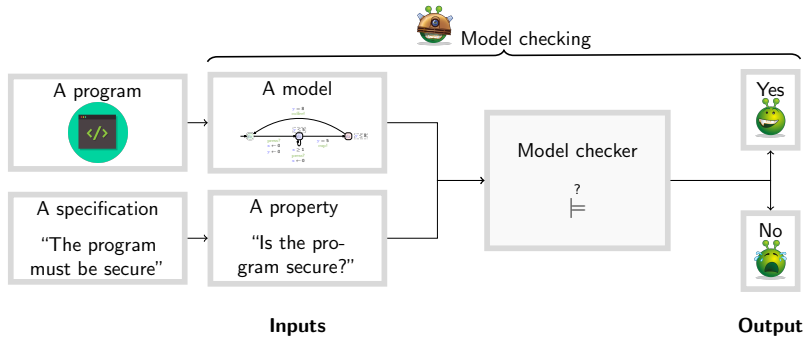
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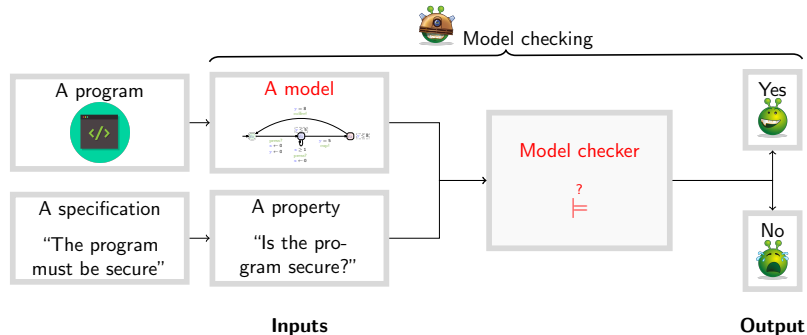
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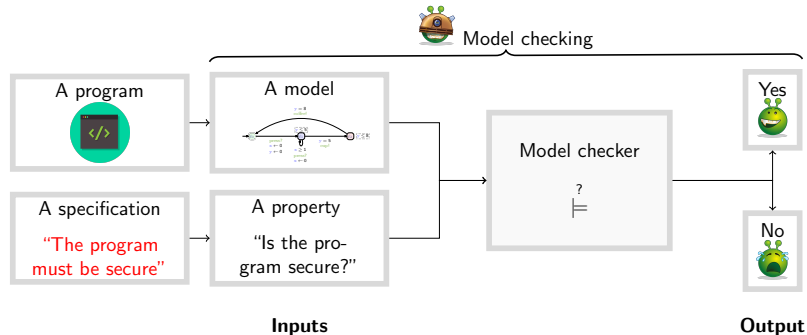
# Outline



## Outline

1. Preliminaries: Timed model checking

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1. Preliminaries: Timed model checking
2. Execution-time opacity

# Outline

Preliminaries: (Parametric) Timed model checking

Execution-time opacity

Expiring ET-opacity problems

Untimed control

Conclusion & Perspectives

# Outline

Preliminaries: (Parametric) Timed model checking

Timed model checking and Timed automata

Parametric timed model checking and Parametric timed automata

Execution-time opacity

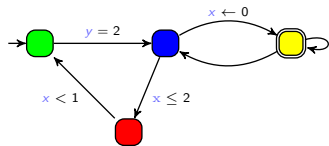
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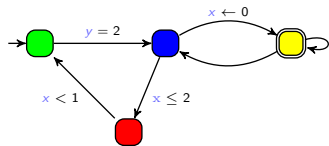
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A **model** of the system

**Red** is unreachable  
A **property** to be satisfied

# Timed model checking



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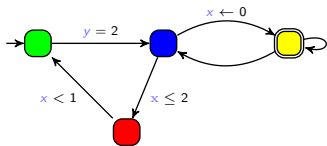
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# Timed model checking



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$\models$

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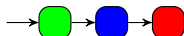
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No

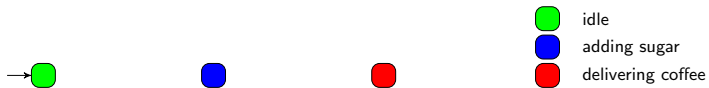


Counterexample

# Timed automaton (TA)

[AD94]

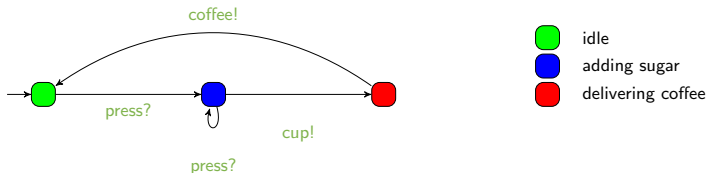
- ▶ Finite state automaton (sets of **locations**)



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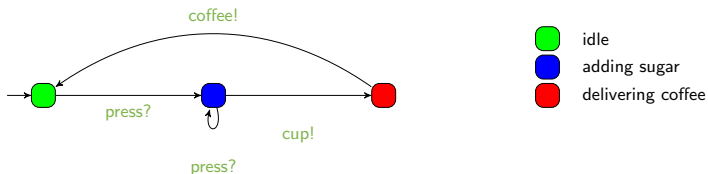
- ▶ Finite state automaton (sets of **locations** and **actions**)



# Timed automaton (TA)

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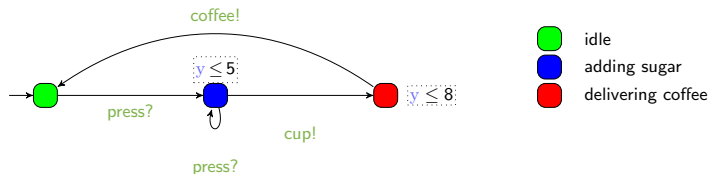
- ▶ Finite state automaton (sets of **locations** and **actions**) augmented with a set  $X$  of **clocks**
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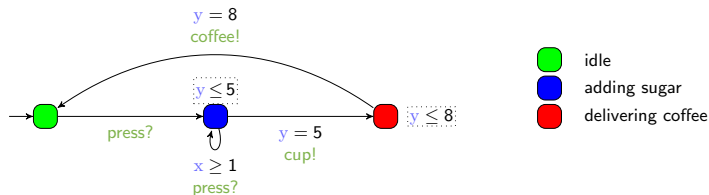
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- ▶ Features
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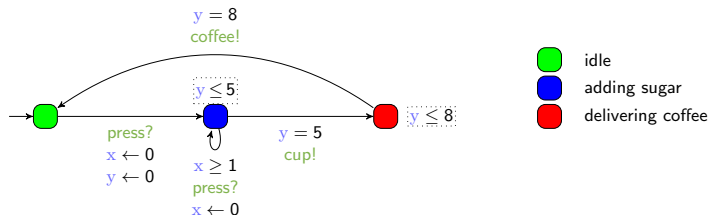




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  - ▶ Transition **guard**: property to be verified to enable a transition
  - ▶ Clock **reset**: some of the clocks can be **set to 0** along transitions



# Outline

## Preliminaries: (Parametric) Timed model checking

Timed model checking and Timed automata

Parametric timed model checking and Parametric timed automata

Execution-time opacity

Expiring ET-opacity problems

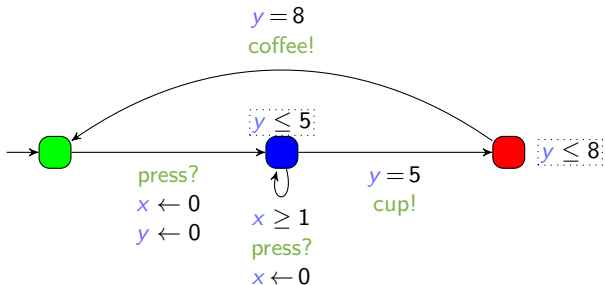
Untimed control

Conclusion & Perspectives

# Timed Automaton (PTA)

[AHV93]

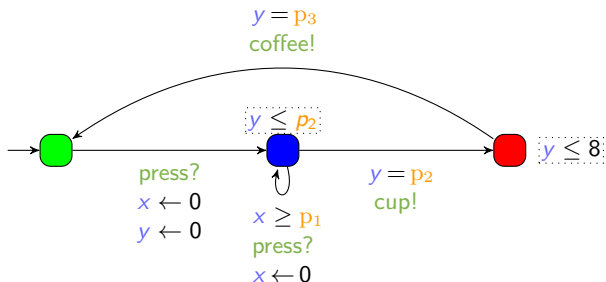
- ▶ Timed automaton (sets of **locations**, **actions** and **clocks**)



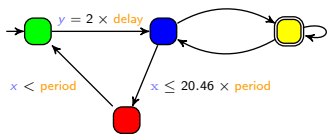
# Parametric Timed Automaton (PTA)

[AHV93]

- ▶ Timed automaton (sets of **locations**, **actions** and **clocks**) augmented with a set  $P$  of **parameters**
  - ▶ **Unknown constants** compared to a **clock** in guards and invariants



# timed model checking



?

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A **property** to be satisfied

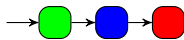
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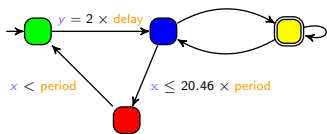


No




Counterexample

# Parametric timed model checking



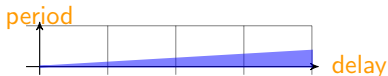
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- ▶ Question: for what values of the parameters does the model of the system **satisfy** the property?

Yes if...



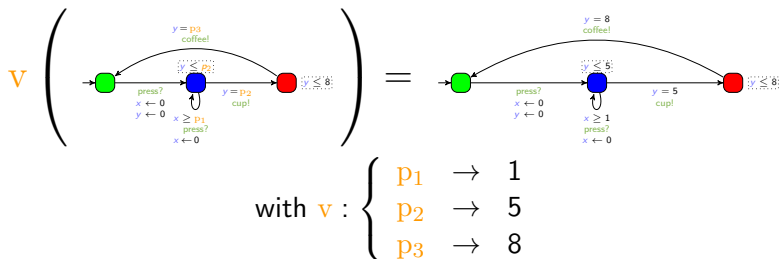
$$2 \times \text{delay} > 20.46 \times \text{period}$$

## Valuation of a PTA = TA

- ▶ Given a PTA  $\mathcal{P}$  and a parameter valuation  $\mathbf{v}$ ,  $\mathbf{v}(\mathcal{P})$  is the TA where each parameter  $\mathbf{p}$  is valued by  $\mathbf{v}(\mathbf{p})$

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Preliminaries: (Parametric) Timed model checking

**Execution-time opacity**

Expiring ET-opacity problems

Untimed control

Conclusion & Perspectives

## Execution-time opacity

- ▶ How to detect timing-leak vulnerabilities?

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- ▶ Check whether a model is secure or not

## Contributions

- ▶ ET-opacity definition, decidability results and experiments [TOSEM22]
- ▶ Expiring ET-opacity definition and decidability results [ICECCS23]
- ▶ Untimed control [FTSCS22]

# Our attacker model

## Attacker capabilities

- ▶ Has access to the model (white box)
- ▶ Can only observe the **total execution time**



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## Attacker goal

- ▶ Wants to deduce some private information based on these observations  
→ visit of a private location

# Outline

Preliminaries: (Parametric) Timed model checking

## Execution-time opacity

- ET-opacity problems in TAs

- ET-opacity problems in PTAs

- Computing ET-opaque durations

Expiring ET-opacity problems

Untimed control

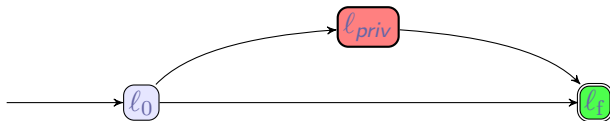
Conclusion & Perspectives

# Formalization

Hypotheses:

[AS19][TOSEM22]

- ▶ A start location  $l_0$  and an end location  $l_f$
- ▶ A special private location  $l_{priv}$



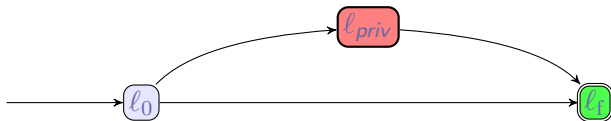


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## Definition (execution-time opacity)

The system is **ET-opaque** for a **duration  $d$**  if there exist two runs to  $l_f$  of duration  $d$

1. one visiting  $l_{priv}$
2. one *not* visiting  $l_{priv}$

## Three levels of ET-opacity

### Existential ( $\exists$ )

There exist a duration  $d$  and two runs of duration  $d$ ,  
one visiting  $\ell_{priv}$ ,  
one not visiting  $\ell_{priv}$

## Three levels of ET-opacity

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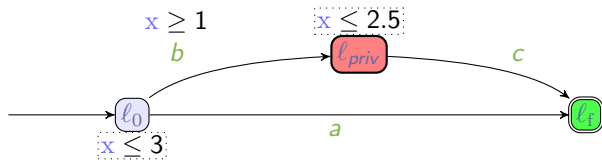
Weak

private durations  $\subseteq$  public durations

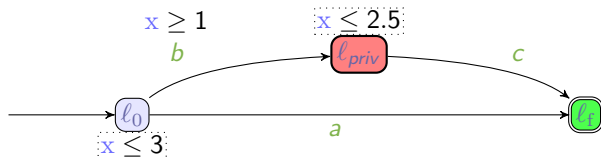
Full

private durations = public durations

# Example



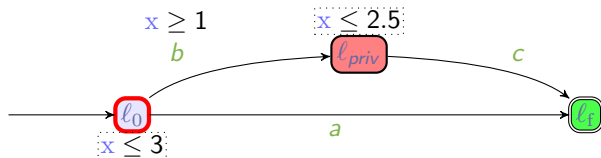
## Example



- ▶ There exist (at least) two runs of duration  $d = 2$ :



# Example

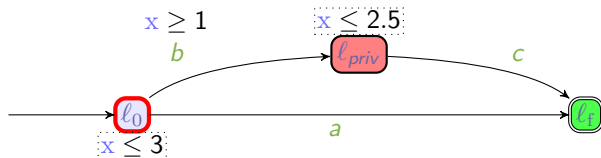


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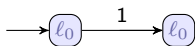


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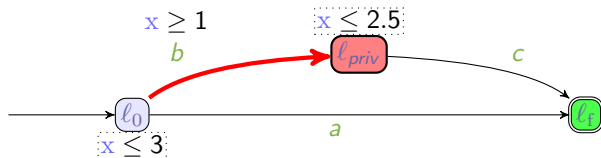


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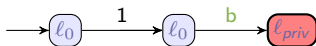


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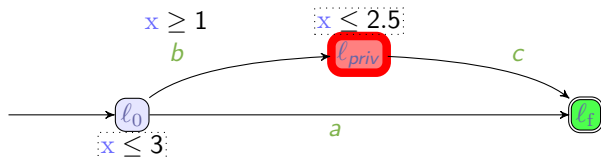


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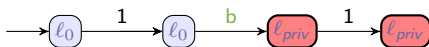


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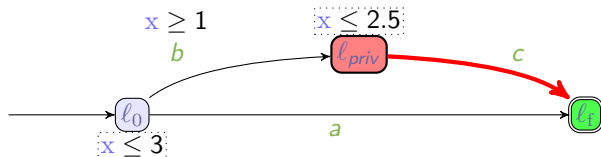


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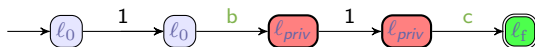


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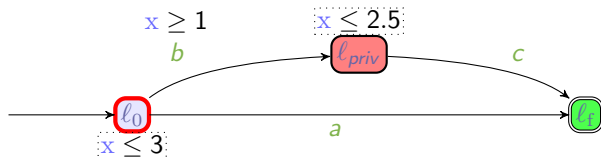


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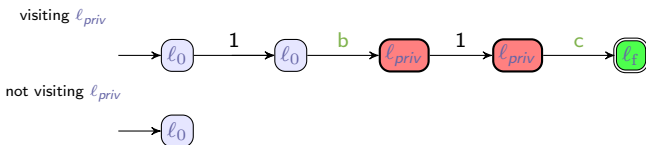
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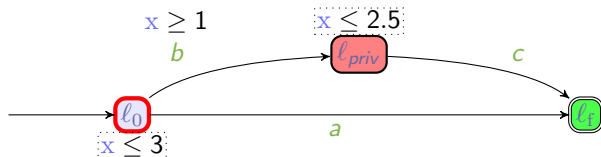
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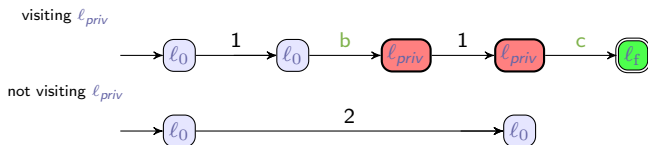
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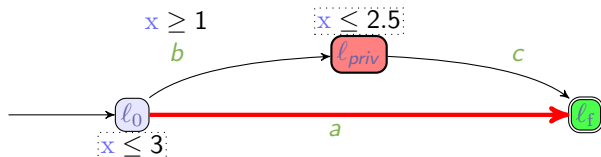
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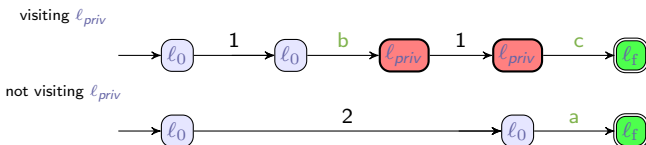
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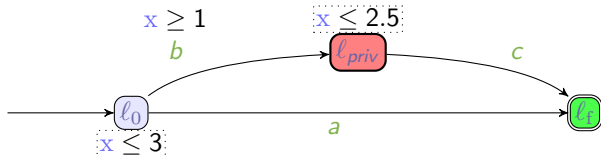


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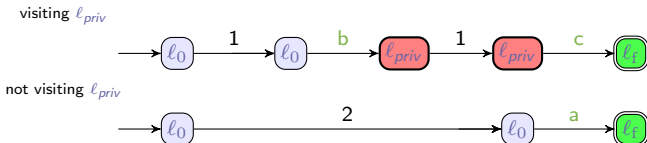




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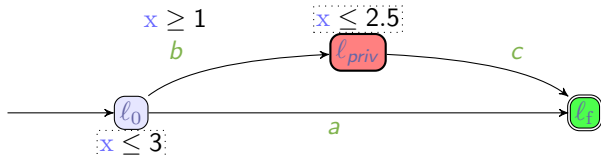
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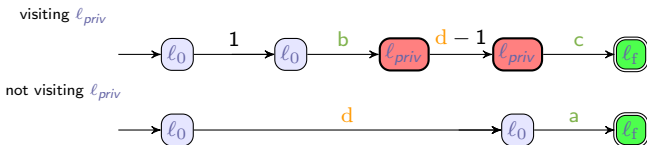
The system is **ET-opaque** for a duration  $d = 2$

The system is  **$\exists$ -ET-opaque**

# Example



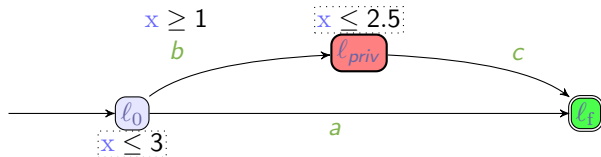
- ▶ There exist (at least) two runs of duration  $d$  for all durations  $d \in [1, 2.5]$ :



The system is **ET-opaque** for all durations in  $[1, 2.5]$

The system is  **$\exists$ -ET-opaque**

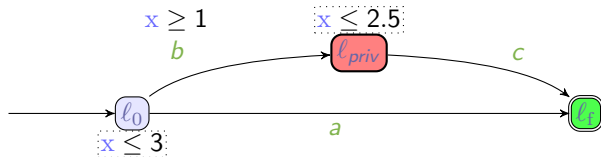
## Example



- ▶ There exist (at least) two runs of duration  $d$  for all durations  $d \in [1, 2.5]$

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## Example

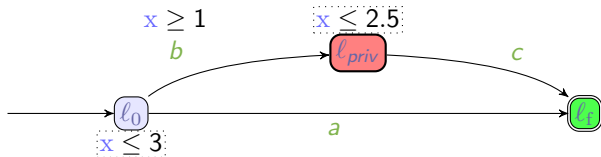


- ▶ There exist (at least) two runs of duration  $d$  for all durations  $d \in [1, 2.5]$

The system is  $\exists$ -ET-opaque

- ▶ private durations are  $[1, 2.5]$   
public durations are  $[0, 3]$

## Example

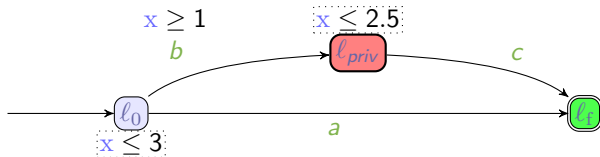


- ▶ There exist (at least) two runs of duration  $d$  for all durations  $d \in [1, 2.5]$

The system is  $\exists$ -ET-opaque

- ▶ private durations are  $[1, 2.5]$   
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- ▶ private durations  $\subseteq$  public durations

## Example



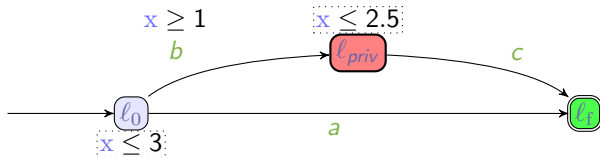
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- ▶ private durations  $\subseteq$  public durations

The system is weakly ET-opaque

## Example



- ▶ There exist (at least) two runs of duration  $d$  for all durations  $d \in [1, 2.5]$

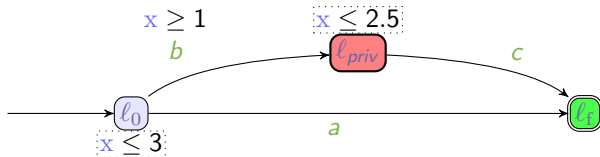
The system is  $\exists$ -ET-opaque

- ▶ private durations are  $[1, 2.5]$   
public durations are  $[0, 3]$
- ▶ private durations  $\subseteq$  public durations

The system is weakly ET-opaque

- ▶ private durations  $\neq$  public durations

## Example



- ▶ There exist (at least) two runs of duration  $d$  for all durations  $d \in [1, 2.5]$

The system is  $\exists$ -ET-opaque

- ▶ private durations are  $[1, 2.5]$   
public durations are  $[0, 3]$
- ▶ private durations  $\subseteq$  public durations

The system is weakly ET-opaque

- ▶ private durations  $\neq$  public durations

The system is not fully ET-opaque



# Outline

Preliminaries: (Parametric) Timed model checking

## Execution-time opacity

ET-opacity problems in TAs

**ET-opacity problems in PTAs**

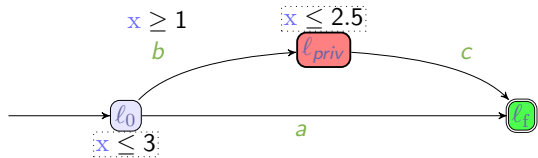
Computing ET-opaque durations

Expiring ET-opacity problems

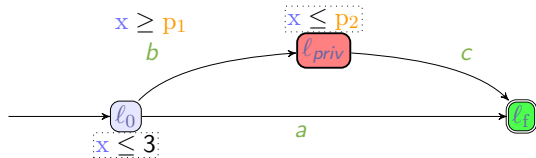
Untimed control

Conclusion & Perspectives

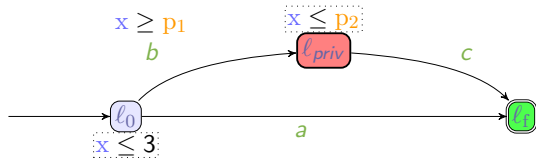
# Example



# Example

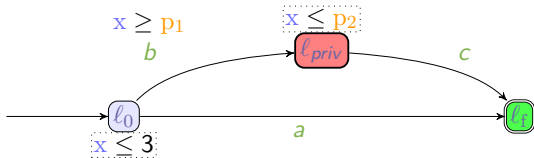


# Example



Private	$[p_1, p_2]$
Public	$[0, 3]$

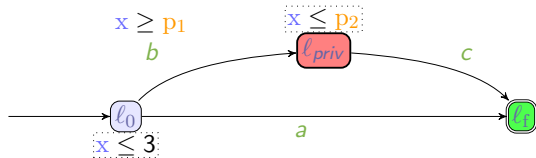
# Example



Private	$[p_1, p_2]$
Public	$[0, 3]$

ET-opacity notion	Private	Public	Answer
$p_1 = 1 \wedge p_2 = 2.5$			
$\exists$			✓
weak	$[1, 2.5]$	$[0, 3]$	✓
full			✗

# Example



Private	$[p_1, p_2]$
Public	$[0, 3]$

ET-opacity notion	Private	Public	Answer
$p_1 = 1 \wedge p_2 = 2.5$			
$\exists$			✓
weak	$[1, 2.5]$	$[0, 3]$	✓
full			✗
$p_1 = 0 \wedge p_2 = 3$			
$\exists$			✓
weak	$[0, 3]$	$[0, 3]$	✓
full			✓

## Two classes of parametric problems

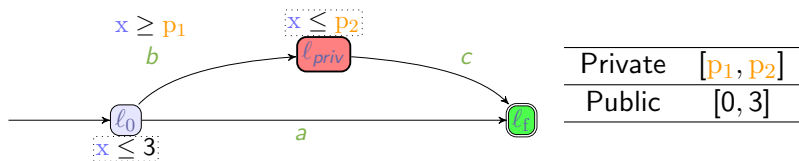
### p-Emptiness problem

Decide the **emptiness** of the set of **parameter valuations**  $v$   
s. t.  $v(\mathcal{P})$  is ET-opaque

### p-Synthesis problem

**Synthesize** the set of **parameter valuations**  $v$   
s. t.  $v(\mathcal{P})$  is ET-opaque

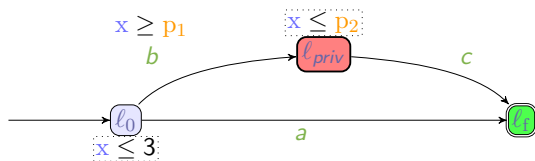
# Example



ET-opacity notion	$\exists$	Weak	Full
<b>p-Emptiness</b>			
<b>p-Synthesis</b>			



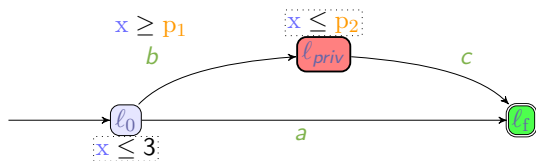
# Example



Private	$[p_1, p_2]$
Public	$[0, 3]$

ET-opacity notion	$\exists$	Weak	Full
$p$ -Emptiness	$\times(\exists v)$	$\times(\exists v)$	$\times(\exists v)$
$p$ -Synthesis			

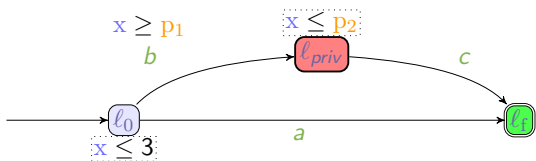
# Example



Private	$[p_1, p_2]$
Public	$[0, 3]$

ET-opacity notion	$\exists$	Weak	Full
$p$ -Emptiness	$\times(\exists v)$	$\times(\exists v)$	$\times(\exists v)$
$p$ -Synthesis	$0 \leq p_1 \leq 3$ $\wedge p_1 \leq p_2$		

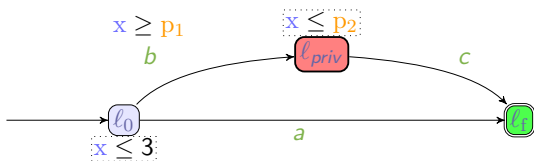
# Example



Private	$[p_1, p_2]$
Public	$[0, 3]$

ET-opacity notion	$\exists$	Weak	Full
$p$ -Emptiness	$\times(\exists v)$	$\times(\exists v)$	$\times(\exists v)$
$p$ -Synthesis	$0 \leq p_1 \leq 3$ $\wedge p_1 \leq p_2$	$0 \leq p_1 \wedge p_2 \leq 3$ $\wedge p_1 \leq p_2$	

# Example



Private	$[p_1, p_2]$
Public	$[0, 3]$

ET-opacity notion	$\exists$	Weak	Full
$p$ -Emptiness	$\times(\exists v)$	$\times(\exists v)$	$\times(\exists v)$
$p$ -Synthesis	$0 \leq p_1 \leq 3$ $\wedge p_1 \leq p_2$	$0 \leq p_1 \wedge p_2 \leq 3$ $\wedge p_1 \leq p_2$	$p_1 = 0 \wedge p_2 = 3$

# Decidability results for ET-opacity

		$\exists$ -ET-opaque	weakly opaque	ET-	fully opaque	ET-
Decision	TA	✓	✓		✓	
$\rho$ -emptiness	L/U-PTA	✓	×		×	
	PTA	×	×		×	
$\rho$ -synthesis	L/U-PTA	×	×		×	
	PTA	×	×		×	

- ▶ **L/U-PTA** (*Lower/Upper-PTA*): subclass of PTA where the parameters are partitioned into two sets (either compared to clocks as upperbound, or as lower bound) [Hun+02]
- ▶ *Proofs are based on the region automaton (for TAs) and by reduction from EF-emptiness (for PTAs). (see formal proofs in Manuscript, Chapter 7)*

# Decidability results for ET-opacity

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Decision	TA	✓	✓		✓	
$\rho$ -emptiness	L/U-PTA	✓	×		×	
	PTA	×	×		×	
$\rho$ -synthesis	L/U-PTA	×	×		×	
	PTA	×	×		×	

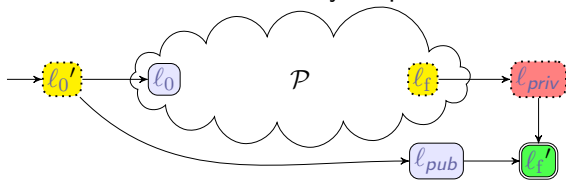
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- ▶ *Proofs are based on the region automaton (for TAs) and by reduction from EF-emptiness (for PTAs). (see formal proofs in Manuscript, Chapter 7)*

# ET-opacity synthesis is (very) difficult

## Theorem (Undecidability of $\exists$ -ET-opacity $p$ -emptiness)

Given  $\mathcal{P}$ , the mere existence of a *parameter valuation*  $v$  s. t.  $v(\mathcal{P})$   $\exists$ -ET-opacity *is undecidable*.

Proof idea: reduction from reachability-emptiness for PTAs



Remark: **L/U-PTA** is a decidable subclass

# Outline

Preliminaries: (Parametric) Timed model checking

## Execution-time opacity

ET-opacity problems in TAs

ET-opacity problems in PTAs

**Computing ET-opaque durations**

Expiring ET-opacity problems

Untimed control

Conclusion & Perspectives



# Experiments: Computing ET-opaque durations

- ▶ Benchmark library + Library of Java programs <sup>2</sup>
  - ▶ Manually translated to PTAs
  - ▶ User-input variables → (non-timing) parameters
- ▶ Algorithms
  1. “Is the TA ET-opaque for all execution times?”
  2. “Synthesize **parameter valuations** and **durations** ensuring ET-opacity of a given PTA”

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<sup>2</sup><https://github.com/Apogee-Research/STAC/>

# Experiments: Computing ET-opaque durations

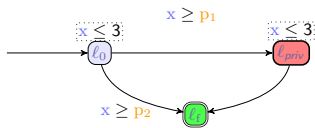
- ▶ Benchmark library + Library of Java programs <sup>2</sup>
    - ▶ Manually translated to PTAs
    - ▶ User-input variables → (non-timing) parameters
  - ▶ Algorithms
    1. “Is the TA ET-opaque for all execution times?”
    2. “Synthesize **parameter valuations** and **durations** ensuring ET-opacity of a given PTA”
- ▶ Problems are undecidable → best-effort approach
  - ▶ Algorithms based on parameter synthesis



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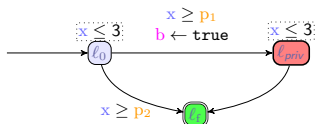
<sup>2</sup><https://github.com/Apogee-Research/STAC/>

# Our transformation of the PTA in 4 overlays



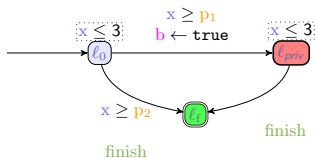
# Our transformation of the PTA in 4 overlays

1. Add a Boolean flag **b**



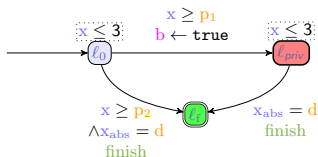
# Our transformation of the PTA in 4 overlays

1. Add a Boolean flag **b**
2. Add a synchronization action **finish**



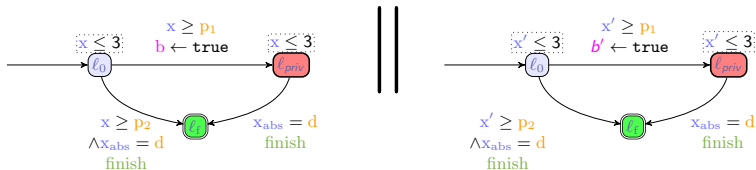
# Our transformation of the PTA in 4 overlays

1. Add a Boolean flag **b**
2. Add a synchronization action **finish**
3. Measure the (parametric) duration to  $\ell_f$



# Our transformation of the PTA in 4 overlays

1. Add a Boolean flag  $b$
2. Add a synchronization action  $finish$
3. Measure the (parametric) duration to  $\ell_f$
4. Perform **self-composition**  
(a synchronization on shared actions of the PTA with a copy of itself)

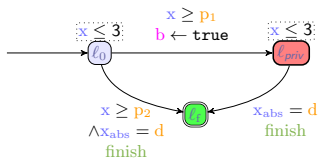


# Applying reachability-synthesis

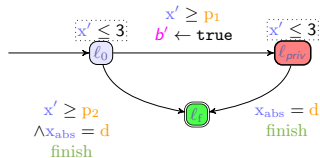
Synthesize all **parameter valuations** (including **d**) with a particular reachable state:

- ▶  $l_f$  with  $b = \text{true}$
- ▶  $l_f$  with  $b' = \text{false}$

$(l_f, b = \text{true})$



$(l_f, b' = \text{false})$



Formal proof of correctness: see [TOSEM22]



# Outline

Preliminaries: (Parametric) Timed model checking

Execution-time opacity

**Expiring ET-opacity problems**

Untimed control

Conclusion & Perspectives

# Expiring ET-opacity

- ▶ How to deal with outdated secrets?  
e. g., cache values, status of the memory, ...



## Idea

The secret can **expire**: beyond a certain duration, knowing the secret is useless to the attacker (e. g., a cache value) [Amm+21]

# Expiring ET-opacity

## Assumption

Knowing an expired secret is equivalent to not knowing a secret

	Secret runs	Non-secret runs
ET-opacity	Runs visiting the private location (= <b>private</b> runs)	Runs not visiting the private location (= <b>public</b> runs)
expiring-ET-opacity	<b>Private</b> runs with $\ell_{priv}$ visit $\leq \Delta$ before the system completion	(i) <b>Public</b> runs and (ii) <b>Private</b> runs with $\ell_{priv}$ visit $> \Delta$ before the system completion

Existential ( $\exists$ )

private durations  $\cap$  public durations  $\neq \emptyset$

Weak

private durations  $\subseteq$  public durations

Full

private durations = public durations

## Three levels of **expiring** ET-opacity

Existential ( $\exists$ ) expiring

**secret** durations  $\cap$  **non-secret** durations  $\neq \emptyset$

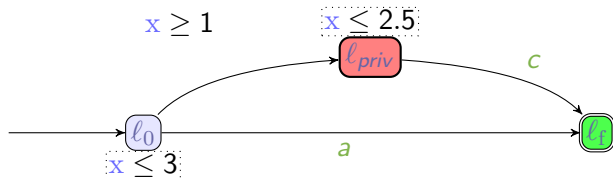
Weak expiring

**secret** durations  $\subseteq$  **non-secret** durations

Full expiring

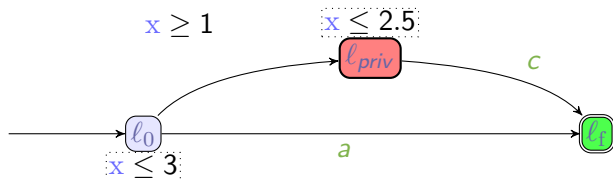
**secret** durations = **non-secret** durations

# Example



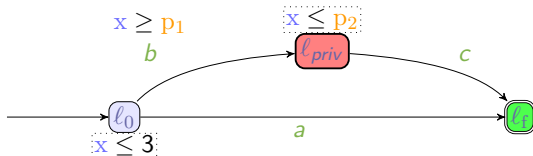
ET-opacity notion	Secret	Non-secret	Answer
$\exists$			✓
weak	[1, 2.5]	[0, 3]	✓
full			×
$\exists$ -exp.			✓
$\Delta = 1$ weak-exp.	[1, 2.5]	$(2, 2.5] \cup [0, 3]$	✓
full-exp.			×

# Example



ET-opacity notion	Secret	Non-secret	Answer
$\exists$			$\checkmark$
weak	[1, 2.5]	[0, 3]	$\checkmark$
full			$\times$
$\exists$ -exp.			$\checkmark$
$\Delta = 1$ weak-exp.	[1, 2.5]	$(2, 2.5] \cup [0, 3]$	$\checkmark$
full-exp.			$\times$
$\exists$ -exp.			$\checkmark$
$\Delta = 1.25$ weak-exp.	[1, 2.5]	$(2.25, 2.5] \cup [0, 3]$	$\checkmark$
full-exp.			$\times$

# Example

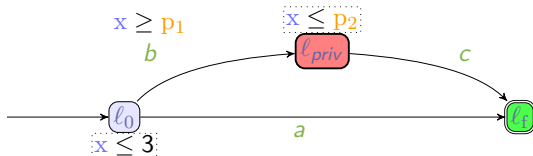


	if $p_1 \leq 3$	otherwise
Secret	$[p_1, \min(\Delta + 3, p_2)]$	$\emptyset$
Non-secret	$(p_1 + \Delta, p_2] \cup [0, 3]$	$\emptyset \cup [0, 3]$

ET-opacity notion	Weak	Full
$(p+\Delta)$ -Emptiness		
$(p+\Delta)$ -Synthesis		



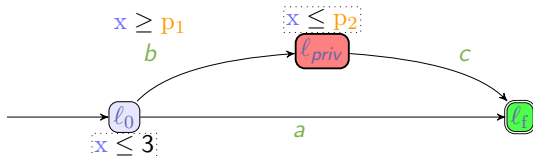
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	if $p_1 \leq 3$	otherwise
Secret	$[p_1, \min(\Delta + 3, p_2)]$	$\emptyset$
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ET-opacity notion	Weak	Full
$(p+\Delta)$ -Emptiness	$\times(\exists v)$	$\times(\exists v)$
$(p+\Delta)$ -Synthesis		

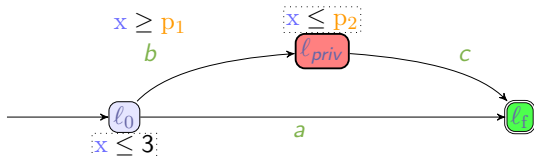
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Secret	$[p_1, \min(\Delta + 3, p_2)]$	$\emptyset$
Non-secret	$(p_1 + \Delta, p_2] \cup [0, 3]$	$\emptyset \cup [0, 3]$

ET-opacity notion	Weak	Full
$(p+\Delta)$ -Emptiness	$\times(\exists v)$	$\times(\exists v)$
$(p+\Delta)$ -Synthesis	$\vee \begin{matrix} p_1 > 3 \\ p_2 \leq 3 \end{matrix} \vee \begin{matrix} \Delta = 0 \\ p_1 + \Delta \leq 3 \end{matrix}$	

# Example



	if $p_1 \leq 3$	otherwise
Secret	$[p_1, \min(\Delta + 3, p_2)]$	$\emptyset$
Non-secret	$(p_1 + \Delta, p_2] \cup [0, 3]$	$\emptyset \cup [0, 3]$

ET-opacity notion	Weak	Full
$(p+\Delta)$ -Emptiness	$\times(\exists v)$	$\times(\exists v)$
$(p+\Delta)$ -Synthesis	$\vee \begin{matrix} p_1 > 3 \\ p_2 \leq 3 \end{matrix} \vee \begin{matrix} \Delta = 0 \\ p_1 + \Delta \leq 3 \end{matrix}$	$p_1 = 0 \wedge ( (\Delta \leq 3 \wedge 3 \leq p_2 \leq \Delta + 3) \vee (p_2 = 3) )$

# Decidability results for expiring-ET-opacity

		weakly expiring- ET-opaque	fully expiring- ET-opaque
$\Delta$ -emptiness	TA	✓	✓
$\Delta$ -synthesis		✓	?
$(p + \Delta)$ -emptiness	L/U-PTA	×	×
	PTA	×	×
$(p + \Delta)$ -synthesis	L/U-PTA	×	×
	PTA	×	×

- ▶  $\exists$ -expiring ET-opacity was left as a future work.
- ▶ **L/U-PTA** (*Lower/Upper-PTA*): subclass of PTA where the parameters are partitioned into two sets (either compared to clocks as upperbound, or as lower bound) [Hun+02]

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# Outline

Preliminaries: (Parametric) Timed model checking

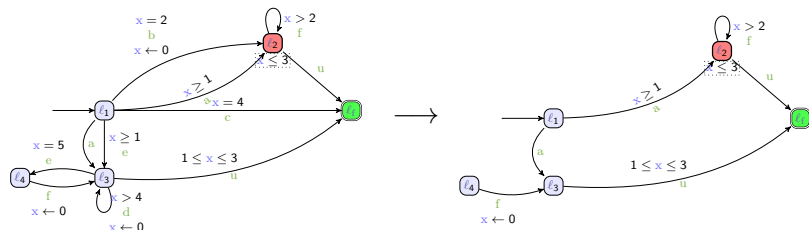
Execution-time opacity

Expiring ET-opacity problems

**Untimed control**

Conclusion & Perspectives

# Untimed control



- ▶ Restrict the behavior of the system to ensure ET-opacity
- ▶ Development of an **open-source** tool **strategFTO** ( $\approx 1200$  lines of code, Java)
  - ▶ Enumeration of transition sets

# Outline

Preliminaries: (Parametric) Timed model checking

Execution-time opacity

Expiring ET-opacity problems

Untimed control

Conclusion & Perspectives



# Conclusion

## Context: vulnerability by timing-attacks

- ▶ Attacker model: observability of the **global execution time**
- ▶ Goal: avoid leaking information on whether some discrete state has been visited

## Several problems studied for timed automata

- 😊 Mostly decidable

## Extension to parametric timed automata

- ☹ Quickly undecidable
- 😊 One procedure for one synthesis problem
- ▶ Toolkit: IMITATOR
- ▶ Benchmarks: concurrent systems and Java programs

# Perspectives

## Theoretical perspectives

- ▶ Existential version of expiring ET-opacity
- ▶  $\Delta$ -synthesis for full expiring ET-opacity

## Algorithmic perspectives

- ▶ Synthesis for weak and full ET-opacity
- ▶ Synthesis for expiring problems

## Automatic translation of programs to PTAs

- ▶ Our translation required non-trivial creativity
  - Preliminary translation with Petri nets including cache system

## References I

- [AD94] Rajeev Alur and David L. Dill. “A theory of timed automata”. In: *TCS* 126 (Apr. 1994).
- [AHV93] Rajeev Alur, Thomas A. Henzinger, and Moshe Y. Vardi. “Parametric real-time reasoning”. In: *STOC* (1993). ACM, 1993.
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- [AS19] Étienne André and Jun Sun. “Parametric Timed Model Checking for Guaranteeing Timed Opacity”. In: *ATVA* (2019). LNCS. Springer, 2019.
- [FTSCS22] Étienne André, Shapagat Bolat, Engel Lefauchaux, and Dylan Marinho. “strategFTO: Untimed control for timed opacity”. In: *FTSCS* (2022). ACM, 2022.

## References II

- [Hun+02] Thomas Hune, Judi Romijn, Mariëlle Stoelinga, and Frits W. Vaandrager. “Linear parametric model checking of timed automata”. In: *Journal of Logic and Algebraic Programming* 52-53 (2002).
- [ICECCS23] Étienne André, Engel Lefaucheux, and Dylan Marinho. “Expiring opacity problems in parametric timed automata”. In: *ICECCS (2023)*. To appear. Springer, 2023.
- [TOSEM22] Étienne André, Didier Lime, Dylan Marinho, and Jun Sun. “Guaranteeing Timed Opacity using Parametric Timed Model Checking”. In: *ACM TOSEM* 31 (2022).

# Licensing

# Source of the graphics used I



Title: Smiley green alien big eyes (aaah)

Author: LadyofHats

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Title: Smiley green alien big eyes (cry)

Author: LadyofHats

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Title: Smiley green alien exterminate

Author: LadyofHats

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Title: Piratey, vector version

Author: Gustavb

Source: [https://commons.wikimedia.org/wiki/File:Piratey,\\_vector\\_version.svg](https://commons.wikimedia.org/wiki/File:Piratey,_vector_version.svg)

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Title: Expired

Author: RRZEicons

Source: <https://commons.wikimedia.org/wiki/File:Expired.svg>

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( $\LaTeX$  source available on demand)

Authors: **Étienne André** and **Dylan Marinho**



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